

2. A)

(a) Assuming the standard quantum mechanical substitutions, derive the Klein-Gordon equation. {4}

(b) Explain why this equation is suitable for describing pions but not quarks. {2}

(c) The Dirac Equation is

$$i\hbar \frac{\partial \Psi(\underline{x}, t)}{\partial t} = H(\underline{x}, \underline{p}) \Psi(\underline{x}, t)$$

$$\text{where } H = -i\hbar c \sum_{i=1}^3 \alpha_i \frac{\partial}{\partial x_i} + \beta mc^2.$$

Show that for a particle at rest

$$\psi_1 = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} e^{-iE_1 t / \hbar} \text{ and } \psi_3 = \begin{pmatrix} 0 \\ 0 \\ 1 \\ 0 \end{pmatrix} e^{-iE_3 t / \hbar}$$

satisfy the Dirac equation and determine the energies  $E_1$  and  $E_3$ .

{6}

$$(A \text{ suitable form for } \beta \text{ is } \beta = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}.)$$

(d) A  $B_s^0$  meson is produced and decays. By drawing Feynman diagrams for each of the following processes, and considering related anti-particle processes, discuss how each process can be used to identify if the meson is a particle or anti-particle at its time of decay.

(i)  $B_s^0 \rightarrow \overline{B_s^0}$  {4}

(ii)  $B_s^0 \rightarrow D_s^- \pi^+$  {4}

(iii)  $\overline{B_s^0} \rightarrow D_s^- K^+$  {4}